

### POZNAN UNIVERSITY OF TECHNOLOGY

**EUROPEAN CREDIT TRANSFER AND ACCUMULATION SYSTEM (ECTS)** 

### **COURSE DESCRIPTION CARD - SYLLABUS**

Course name

Mathematics [S1MiBM2>MAT1]

Course

Field of study Year/Semester

Mechanical Engineering 1/1

Area of study (specialization) Profile of study

general academic

Level of study Course offered in

first-cycle Polish

Form of study Requirements full-time compulsory

**Number of hours** 

Lecture Laboratory classes Other (e.g. online)

45 0

Tutorials Projects/seminars

30 0

Number of credit points

5,00

Coordinators Lecturers

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### **Prerequisites**

• Knowledge of mathematics at the secondary school level • Ability to think logically • Proficiency in using mathematical tools from secondary school to solve tasks • Capacity to learn with understanding • Ability to independently search for information in literature

# Course objective

Learning about the applications of mathematical tools and methods to solve simple technical problems and indicating the possibilities of using mathematics in more complex problems.

### Course-related learning outcomes

none

## Methods for verifying learning outcomes and assessment criteria

Learning outcomes presented above are verified as follows:

Lecture: assessment of knowledge and skills demonstrated in the written exam. The exam is assessed in a point system. The condition of passing the exam is obtaining at least 50% of points.

Tutorials: two written assignments carried out under the teacher's supervision. The condition of receiving a positive grade from tutorials is obtaining at least 50% of points. Additional points can be obtained for activity during classes.

## Programme content

- 1. LINEAR ALGEBRA
- 2. ELEMENTS OF ANALITYCAL GEOMETRY
- 3. FUNCTIONS AND THEIR PROPORTIES
- 4. SEQUENCES
- 5. LIMITS AND CONTINUITY OF FUNCTIONS
- 6. DERIVATIVE OF FUNCTION
- 7. INDEFINITE INTEGRALS
- 8. DEFINITE AND IMPROPER INTEGRALS
- 9. COMPLEX NUMBERS
- 10. INFINITE SERIES AND POWER SERIES

### **Course topics**

#### Lecture:

- 1. LINEAR ALGEBRA
- matrix (definition, basis notations and examples)
- matrix operations (addition, subtraction, scalar multiplication, transposition, matrix multiplication, matrix inverse)
- determinants (definition, Sarrus' rule, Laplace expansion, propertis of determinants)
- 2. ELEMENTS OF ANALITYCAL GEOMETRY
- · vectors in three dimensions
- vector calculus (addition, multiplication by scalar, dot product, cross product, mixed product)
- parallel and perpendicular vectors
- area formulas for parallelogram/triangle and parallelepiped/tetrahedron spanned by vectors
- angle between two vectors
- 3. FUNCTIONS AND THEIR PROPORTIES
- definition of function, domain and range of function, graph of function
- bounded function, increasing and decreasing functions, periodic function, even and odd functions, function composition
- surjection, injection, inverse function
- natural logarithm, cyclometric functions, hyperbolic function, area functions
- implicit function, parametric representation of curve, curves in polar coordinates
- 4. SEQUENCES
- definition of sequence
- bounded sequence, monotone sequence
- limit of sequence (including Euler's number), convergent and divergent sequences
- theorems of sequences (including arithmetic rule, the squeeze theorem)
- 5. LIMITS AND CONTINUITY OF FUNCTIONS
- · definitions of limits
- properties of limits, theorems on limits (including arithmetic rule, the squeeze theorem)
- indeterminate forms
- continuous functions and their properties (including Weierstrass theorem and Darboux's theorem)
- · discontinuous functions
- 6. DERIVATIVE OF FUNCTION
- definition of derivative, geometric interpretation of derivative, right and left-hand derivatives, theorems of derivatives, properties and rules for funding derivatives
- tangent and normal lines
- · increments and differentials
- L'Hospital's rule
- higher order derivatives

- · horizontal and vertical asymptotes
- ekstrema of functions
- the first derivative test
- · concavity and the secound derivative test
- applications of extrema

#### 7. INDEFINITE INTEGRALS

- antiderivative of function, properties of integration (including integration by parts, change of variable)
- integration of rational function, method of partial fractions
- trigonometric substitutions, integration of some irrational functions

### 8. DEFINITE AND IMPROPER INTEGRALS

- definition of definite integral, Riemann sum, geometric interpretation of definite integral, fundamental theorem of integral calculus
- properties of the definite integral (including integration by parts, change of variable)
- applications of the definite integral (including area, volume and surface area of solids of revolution, length of curve)
- improper integrals (integrals with infinite limits of integration, integrals with discontinuous integrands)

#### 9. COMPLEX NUMBERS

- modulus, argument, principal argument
- forms: geometric, rectangular, polar (complex plane)
- square root of complex number
- quadratic equation in the complex domain
- deriving polar form from rectangular form
- de Moivre's formula
- formula for the n-th root of a complex number
- · multiplication and division of complex numbers in polar form
- Euler's formula for complex numbers

#### 10. INFINITE SERIES AND POWER SERIES

- definition of infinite series, sum of the series, necessary condition for convergence, convergent or divegent infinite series
- convergence tests (integral test, comparison test, alternating series test, ratio test, root test)
- absolute and conditional convergence
- power series, radius of convergence, interval of convergence
- power series representations of functions
- Taylor and Maclaurin series and applications

#### **Tutorials:**

#### 1. LINEAR ALGEBRA

- matrix operations (addition, subtraction, scalar multiplication, transposition, matrix multiplication, matrix inverse)
- determinants (Sarrus' rule, Laplace expansion, propertis of determinants)

#### 2. ELEMENTS OF ANALITYCAL GEOMETRY

- vectors in three dimensions
- vector calculus (addition, multiplication by scalar, dot product, cross product, mixed product)
- parallel and perpendicular vectors
- area formulas for parallelogram/triangle and parallelepiped/tetrahedron spanned by vectors
- · angle between two vectors

#### 3. FUNCTIONS AND THEIR PROPORTIES

- domain and range of function, graph of function
- bounded function, increasing and decreasing functions, periodic function, even and odd functions, function composition
- inverse function
- natural logarithm, cyclometric functions, hyperbolic function, area functions

#### 4. SEQUENCES

- bounded sequence, monotone sequence
- limit of sequence (including Euler's number), convergent and divergent sequences
- theorems of sequences (including arithmetic rule, the squeeze theorem)

### 5. LIMITS AND CONTINUITY OF FUNCTIONS

- properties of limits, theorems on limits (including arithmetic rule, the squeeze theorem)
- indeterminate forms
- continuous functions and their properties

#### 6. DERIVATIVE OF FUNCTION

- definition of derivative, theorems of derivatives, properties and rules for funding derivatives
- tangent and normal lines
- · increments and differentials
- L'Hospital's rule
- higher order derivatives
- · horizontal and vertical asymptotes
- · ekstrema of functions
- the first derivative test
- · concavity and the secound derivative test
- applications of extrema
- 7. INDEFINITE INTEGRALS
- antiderivative of function, properties of integration (including integration by parts, change of variable)
- integration of rational function, method of partial fractions
- trigonometric substitutions
- 8. DEFINITE INTEGRALS
- fundamental theorem of integral calculus
- properties of the definite integral (including integration by parts, change of variable)
- applications of the definite integral (including area)

# **Teaching methods**

Lecture: mulimedia presentation accompanied with examples presented on the blackboard and with questions to the group of students

Tutorials: solving problems on the board, initiating discassion about the solutions

## **Bibliography**

#### Basic:

- 1. M. Gewert, Z. Skoczylas, Analiza Matematyczna 1 i 2, Definicje, twierdzenia i wzory, Oficyna Wydawnicza GiS, Wrocław 2019.
- 2. M. Gewert, Z. Skoczylas, Analiza Matematyczna 1 i 2, Przykłady i zadania, Oficyna Wydawnicza GiS, Wrocław 2018.
- 3. W. Krysicki, L. Włodarski, Analiza matematyczna w zadaniach cz. I, Wydawnictwo Naukowe PWN, Warszawa 2015.
- 4. W. Żakowski, W. Kołodziej, Matematyka cz. II, Analiza matematyczna, WNT, Warszawa 2017.
- 5. W. Żakowski, G. Decewicz, Matematyka cz. I, Analiza matematyczna, WNT, Warszawa 2017.
- 6. T. Jurlewicz, Z. Skoczylas, Algebra liniowa 1, Definicje, twierdzenia, wzory, Oficyna Wydawnicza GiS, Wrocław 2002.
- 7. T. Jurlewicz, Z. Skoczylas, Algebra liniowa 1, Przykłady i zadania, Oficyna Wydawnicza GiS, Wrocław 2006.

## Breakdown of average student's workload

	Hours	ECTS
Total workload	125	5,00
Classes requiring direct contact with the teacher	77	3,00
Student's own work (literature studies, preparation for laboratory classes/ tutorials, preparation for tests/exam, project preparation)	48	2,00